



1.) label all nodes with letter subscripts

2.) label resistors, their voltage drops and branch currents with current subscripts

knowns:

$$R_1 := 1000$$

$$R_2 := 2000$$

$$R_3 := 3000$$

$$R_4 := 4000$$

$$R_5 := 5000$$

$$V_0 := 1200$$

3.) first set of equations is describing voltage drops in terms of node voltages... source minus destination as described by arbitrary

$$V_1 := V_A - V_B \quad V_A := V_0$$

$$V_2 := V_B - V_C$$

$$V_3 := V_B - 0$$

$$V_4 := V_C - 0$$

$$V_5 := V_A - V_C$$

4.) ohms law to describe currents.

$$I_1 := \frac{V_1}{R_1} \xrightarrow{\text{factor}} \frac{V_A - V_B}{1000} \quad I_2 := \frac{V_2}{R_2} \xrightarrow{\text{factor}} \frac{V_B - V_C}{2000} \quad I_3 := \frac{V_3}{R_3} \xrightarrow{\text{factor}} \frac{V_B}{3000}$$

$$I_4 := \frac{V_4}{R_4} \xrightarrow{\text{factor}} \frac{V_C}{4000} \quad I_5 := \frac{V_5}{R_5} \xrightarrow{\text{factor}} -\frac{V_C - 1200}{5000}$$

## 5.) nodal conservation equations

Do the conservation equations here because you need the bold equal sign to put more than one term on the left hand side of any equation should it be called for.

$$\begin{bmatrix} I_0 = I_1 + I_5 \\ I_1 = I_2 + I_3 \\ I_4 = I_2 + I_5 \end{bmatrix} \rightarrow \begin{bmatrix} I_0 = \frac{36}{25} - \frac{V_C}{5000} - \frac{V_B}{1000} \\ \frac{6}{5} - \frac{V_B}{1000} = \frac{V_B}{1200} - \frac{V_C}{2000} \\ \frac{V_C}{4000} = \frac{V_B}{2000} - \frac{7 \cdot V_C}{10000} + \frac{6}{25} \end{bmatrix}$$

why won't it solve?

the simultaneous equations apparently substitute in variables properly so what's the problem?

$$\begin{bmatrix} I_0 = I_1 + I_5 \\ I_1 = I_2 + I_3 \\ I_4 = I_2 + I_5 \end{bmatrix} \xrightarrow{\text{solve}, I_0, V_B, V_C} \begin{bmatrix} 408 & 151200 & 124800 \\ 895 & 179 & 179 \end{bmatrix} = [0.456 \quad 844.693 \quad 697.207]$$

### Troubleshooting:

Mathcad prime apparently doesn't like me variables, even after clearing them.

`clear(VC)`      `clear(VB)`      `clear(I0)`

$V_C \rightarrow V_C$        $V_B \rightarrow V_B$        $I_0 \rightarrow I_0$

$V_C = ?$        $V_B = ?$        $I_0 = ?$

$$\begin{bmatrix} I_0 = \frac{36}{25} - \frac{V_C}{5000} - \frac{V_B}{1000} \\ \frac{6}{5} - \frac{V_B}{1000} = \frac{V_B}{1200} - \frac{V_C}{2000} \\ \frac{V_C}{4000} = \frac{V_B}{2000} - \frac{7 \cdot V_C}{10000} + \frac{6}{25} \end{bmatrix} \xrightarrow{\text{solve}, I_0, V_B, V_C} ?$$

I assume it is the variables because after using more generic ones the solution is forthcoming

$$\begin{bmatrix} x = \frac{36}{25} - \frac{z}{5000} - \frac{y}{1000} \\ \frac{6}{5} - \frac{y}{1000} = \frac{y}{1200} - \frac{z}{2000} \\ z = \frac{y}{2000} - \frac{7 \cdot z}{10000} + \frac{6}{25} \end{bmatrix} \xrightarrow{\text{solve}, x, y, z, \text{float}, 3} [0.456 \quad 845.0 \quad 697.0]$$

[ 4000 2000 10000 25 ]

Known good solutions:

My Casio calculator eats these simultaneous equations right up, as usual...

$$\begin{cases} I_0 = \frac{36}{25} - \frac{V_3}{5000} - \frac{V_2}{1000} \\ \frac{6}{5} - \frac{V_2}{1000} = \frac{V_2}{1200} - \frac{V_3}{2000} \\ \frac{V_3}{4000} = \frac{V_2}{2000} - \frac{7 \cdot V_3}{10000} + \frac{6}{25} \end{cases} \quad I_0, V_2, V_3$$

$$\{I_0=0.4558659218, V_2=844.6927374, V_3=697.2067039\}$$

Which matches the simulation

