

For Maple notation $arctan(u) := atan(u)$ $_C1 := C$

Maple differential equation solver $ode := \frac{d}{d\,x} y(x) - \frac{y(x) - x}{y(x) + x}$ $dsol := maple\big(lhs\big(dsolve\big(ode, y(x)\big)\big)\big)$

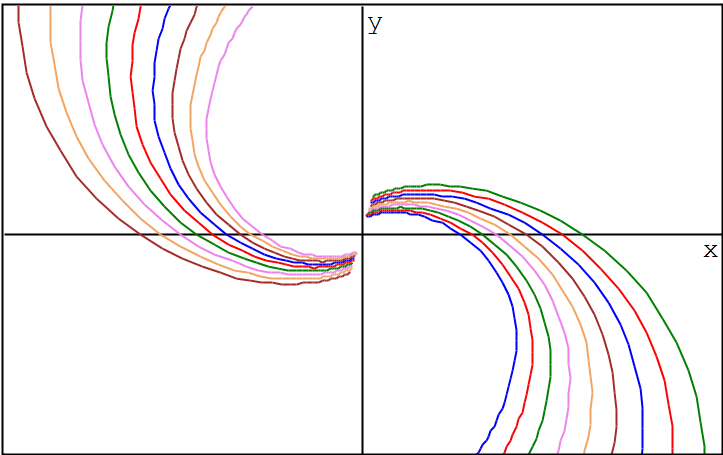
Parametric solution For an homogeneous equation: $y(x) := u \cdot x$

$$x(u, C) := e^{maple\big(solve\big(dsol, \ln(x)\big)\big)}$$

$$y(u, C) := u \cdot x(u, C)$$

Discretizing for plot:

$$\left[\begin{array}{l} Co := 0.1 \cdot [-4..4] \quad n_c := rows(Co) \\ U := [-3, -2.9..5] \quad n := [1..rows(U)] \\ k := [1..n_c] \quad k_2 := k + n_c \\ X_{n\,k} := x(U_{n\,}, Co_{k\,}) \quad Y_{n\,k} := y(U_{n\,}, Co_{k\,}) \\ M_k := augment(X_{n\,k\,}, Y_{n\,k\,}) \quad M_{k_2} := -M_{k_2 - n_c} \\ \Pi := mat2sys_1(M) \end{array} \right]$$

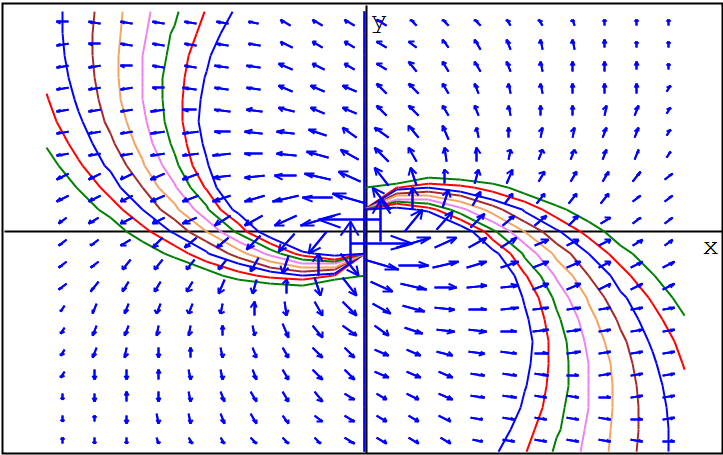


Implicit Solution $y(x) := y$ $f(x, y) := maple\big(solve\big(dsol, C\big)\big)$

Can plot it using vfield library with pVField and pIPlot.

▣—vfield—

$$\left[\begin{array}{l} Grad(x, y) := \left[\frac{d}{d\,x} f(x, y) \quad \frac{d}{d\,y} f(x, y) \right]^T \\ L := \begin{bmatrix} 1 \\ 1 \end{bmatrix} \quad sf(t) := t^{0.6} \quad B := \begin{bmatrix} -2 & 2 \\ -2 & 2 \end{bmatrix} \quad N := \begin{bmatrix} 20 \\ 20 \end{bmatrix} \\ \Pi := \begin{cases} pVField(Grad(x, y), B, N, L, sf(t)) \\ pIPlot(f(x, y), B, N, Co) \end{cases} \end{array} \right]$$



Symbolic Solutions Showing Maple results, they are

Implicit

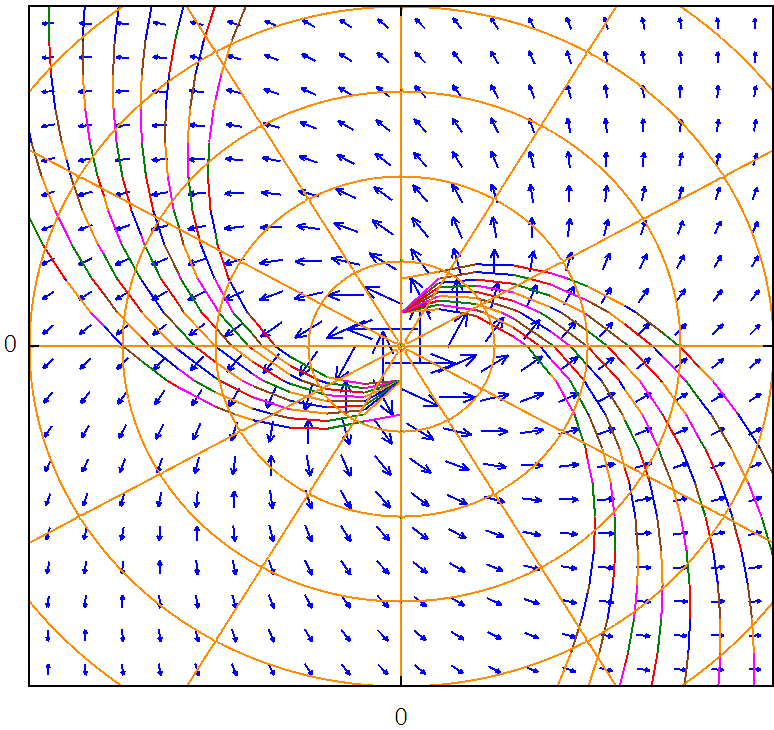
$$f(x, y) = \frac{\ln(y^2 + x^2) + 2 \cdot atan\left(\frac{y}{x}\right)}{2}$$

Parametric

$$\left[\begin{array}{l} x(u, C) \\ y(u, C) \end{array} \right] = \left[\begin{array}{l} \frac{1}{e^{\frac{-2 \cdot C + \ln(1 + u^2) + 2 \cdot atan(u)}{2}}} \\ \frac{u}{e^{\frac{-2 \cdot C + \ln(1 + u^2) + 2 \cdot atan(u)}{2}}} \end{array} \right]$$

$$\varphi\left(x,y\right):=\sin\left(\frac{\pi}{\Delta r}\cdot\sqrt{x^2+y^2}\right)\cdot\sin\left(\frac{180^\circ}{\Delta\varphi}\cdot\operatorname{atan}\left(\frac{y}{x}\right)\right)$$

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Δr := 0.5
Δφ := 30 °
Π3 := ""
Π4 := φ(x,y)
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Alvaro