

My current method

$$C_1 := 1 \text{ }\mu\text{F} \cdot (1 \pm 20 \text{ } \%) = \begin{cases} 1.2 \\ 0.8 \end{cases} \text{ }\mu\text{F} \quad L_1 := 1 \text{ }\mu\text{H} \cdot (1 \pm 5 \text{ } \%) = \begin{cases} 1.05 \\ 0.95 \end{cases} \text{ }\mu\text{H}$$

$$F_1 := \frac{1}{\sqrt{L_1 \cdot C_1}} = \begin{cases} 890.8708 \\ 936.5858 \\ 1091.0895 \\ 1147.0787 \end{cases} \text{ kHz}$$

$$\text{for } i := 1, i \leq 4, i := i + 1 \\ F_{1M} \quad i \quad 1 := F_1 \quad i$$

$$F_{1Range} := \left(\frac{\max(F_{1M}) + \min(F_{1M})}{2} \right) \pm \left(\frac{\max(F_{1M}) - \min(F_{1M})}{2} \right) = \begin{cases} 1147.0787 \\ 890.8708 \end{cases} \text{ kHz}$$

Proposed Method

$$C_2 := 1 \text{ }\mu\text{F} \quad Tol_{C_2} := 20 \text{ }\%$$

$$L_2 := 1 \text{ }\mu\text{H} \quad Tol_{L_2} := 5 \text{ }\%$$

$$F_1 := \frac{1}{\sqrt{L_2 \cdot C_2}} \cdot \left(1 \pm \sqrt{Tol_{C_2}^2 + Tol_{L_2}^2} \right) = \begin{cases} 1206.1553 \\ 793.8447 \end{cases} \text{ kHz}$$

Error propagation Method

Measures and errors $C_2 := 1 \mu\text{F}$ $\Delta C_2 := 20 \% \cdot C_2$ $L_2 := 1 \mu\text{H}$ $\Delta L_2 := 5 \% \cdot L_2$

Only for show $C_2 \pm \Delta C_2 = \begin{cases} 1.2 \\ 0.8 \end{cases} \mu\text{F}$ $L_2 \pm \Delta L_2 = \begin{cases} 1.05 \\ 0.95 \end{cases} \mu\text{H}$

Propagation of errors: given the functional dependency $z=f(x,y)$ the error Δz is

$$\Delta z = \left| \frac{d}{d x} f(x, y) \right| \cdot \Delta x + \left| \frac{d}{d y} f(x, y) \right| \cdot \Delta y$$

In your case: $F(C, L) := \frac{1}{\sqrt{L \cdot C}}$ $F_2 := F(C_2, L_2) = 1000 \text{ kHz}$

$$\Delta F_2 := \left| \frac{d}{d C_2} F(C_2, L_2) \right| \cdot \Delta C_2 + \left| \frac{d}{d L_2} F(C_2, L_2) \right| \cdot \Delta L_2 = 125 \text{ kHz}$$

Finally $F_2 \pm \Delta F_2 = \begin{cases} 1125 \\ 875 \end{cases} \text{ kHz}$

As percent of the value $\Delta \% F_2 := \frac{\Delta F_2}{F_2} = 12.5 \%$

You can put that as procedures
$$Err(X) := \begin{bmatrix} \Delta x := 0.5 \cdot (X_1 - X_2) \\ X_1 - \Delta x \quad \Delta x \end{bmatrix}$$

$$Err(f(1), X) := \begin{bmatrix} x \quad \Delta x \end{bmatrix} := Err(X) \left| \frac{d}{d x} f(x) \right| \cdot \Delta x$$

$$Err(f(2), X, Y) := \begin{bmatrix} x \quad \Delta x \end{bmatrix} := Err(X) \begin{bmatrix} y \quad \Delta y \end{bmatrix} := Err(Y) \left| \frac{d}{d x} f(x, y) \right| \cdot \Delta x + \left| \frac{d}{d y} f(x, y) \right| \cdot \Delta y$$

$$Err(f(3), X, Y, Z) := etc$$

Then $\Delta F_2 := Err(F(C, L), C_2 \pm \Delta C_2, L_2 \pm \Delta L_2) = 125 \text{ kHz}$

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